

## Section A

Transformations of Graphs
Grade A*

1. The diagram shows the graph of $y=x^{2}$ for $-2 \leq x \leq 2$.


Each of the graphs below is a transformation of this graph.
Write down the equation of each graph.
(a)

(b)

(c)

$\qquad$
Answer (c) $y=$
2. The diagrams, which are not drawn to scale, show the graph of $y=x^{2}$ and four other graphs $A, B, C$ and $D$.
$A, B, C$ and $D$ represent four different transformations of $y=x^{2}$.
Find the equation of each of the graphs $A, B, C$ and $D$.


Answer Graph $A$ is $y=$ $\qquad$


Answer Graph $B$ is $y=$


Answer Graph $D$ is $y=$ $\qquad$

Answer Graph $C$ is $y=$ $\qquad$
3. The sketch below is of the graph of $y=x^{2}$


On the axes provided, sketch the following graphs.
The graph of $y=x^{2}$ is shown dotted on each set of axes to act as a guide.
(a) $y=x^{2}+2$

(b) $y=(x-2)^{2}$

(c) $y=\frac{1}{2} x^{2}$

4. $\quad A(1,1)$ and $B(-2,4)$ are two points on the graph of $y=x^{2}$


Here are three transformations of the graph $y=x^{2}$.
On each diagram the graph of $y=x^{2}$ is shown dotted.
The images $A^{\prime}$ and $B^{\prime}$ of $A$ and $B$ are shown.
Write down the equation of the transformed graph in each case.
(a)

(b)

(c)

5. The diagram shows the graph of a function $y=\mathrm{f}(x)$.


On the axes below sketch the graphs of each of these functions. In each case, the graph of $y=\mathrm{f}(x)$. is shown to help you.
(a) $y=\mathrm{f}(x)+2$

(b) $\quad y=2 \mathrm{f}(x)$

(c) $y=\mathrm{f}(2 x)$

6. (a) The graph $y=x^{2}$ is transformed as shown.



Not drawn accurately

Write down the equation of the transformed graph.

$$
\text { Answer } y=
$$

(b) The graph of $y=3 x-2$ is sketched below.


On the same axes, sketch the graph of $y=2-3 x$

| Success: |
| :--- |
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|  |
|  |

Target:

## Section B Transformations of Trigonometric Graphs Grade A＊

1．This is the graph of $y=\cos x$ for $0^{\circ} \leq x \leq 360^{\circ}$


Write the equation of each of the transformed graphs． In each case the graph of $y=\cos x$ is shown dotted to help you．
（a）


Equation $y=$
（b）


Equation $y=$ $\qquad$
（c）


Equation $y=$
(d)


Equation $y=$


Draw the graphs indicated for $0^{\circ} \leq x \leq 360^{\circ}$
In each case the graph of $y=\sin x$ is shown to help you.
(a) $y=2 \sin x \quad$ (1)
(b) $y=-\sin x$
(1)
(c) $y=\sin 2 x$
(1)



3. This is the graph of $y=\cos x$ for $0^{\circ} \leq x \leq 360^{\circ}$

(a) On the axes below draw the graph of $y=\cos (x-90)$ for $0^{\circ} \leq x \leq 360^{\circ}$

(b) Write down a possible equation of the following graph.


Answer
4. This is the graph of $y=\sin x$.


On the grid below, sketch the graph of $y=\sin \left(x-90^{\circ}\right)$

(Total 2 marks)
5. The graph of $y=\sin x$ for $0^{\circ} \leq x \leq 360^{\circ}$ is shown on the grid below.

The point $P(90,1)$ lies on the curve.


On both of the grids that follow, sketch the graph of the transformed function. In both cases write down the coordinates of the transformed point $P$.
(a) $y=\sin (x-45)$

(b) $y=2 \sin x$

6. You are given that $\sin 70^{\circ}=0.9397$
(a) On the axes below sketch the graph of $y=\sin 2 x$ for $0^{\circ} \leq x \leq 360^{\circ}$

(b) Hence write down the four solutions of the equation $\sin 2 x=0.9397$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


## Success:

## Target:

## Section C

Shapes of Graphs

1．Match three of these equations with the graphs shown below．

$$
\begin{aligned}
& y=x+3 \\
& y=3 x \\
& y=3 x^{2} \\
& y=x^{2}+3 \\
& y=3-x^{2}
\end{aligned}
$$




Answer $y=$ $\qquad$ （1）
Answer $y=$
（1）


Answer $y=$
（1）
2. Each of the graphs represents one of the following equations.

$$
\begin{array}{ll}
\hline \mathrm{A} \quad y=3 x+4 \\
\hline \mathrm{C} y=x^{2}-2 & \begin{array}{|l}
\mathrm{B} \quad 2 x+3 y=12 \\
\hline \mathrm{D} \quad y=x^{3} \\
\hline
\end{array} \\
\hline
\end{array}
$$

Write down the letter of the equation represented by each graph


Equation


Equation $\qquad$


Equation $\qquad$
3. (a) Four graphs are sketched.


Graph $A$


Graph $B$


Graph $D$

Complete the following statements.

$$
\begin{array}{ll}
y=2 x+4 & \text { matches graph } \ldots \ldots \ldots \ldots \ldots \ldots \ldots \\
y=x^{2}+4 & \text { matches graph } \ldots \ldots \ldots \ldots \ldots \ldots \ldots \\
y+2 x=4 & \text { matches graph } \ldots \ldots \ldots \ldots \ldots \ldots \ldots .
\end{array}
$$

(b) Sketch the graph of $y=x^{3}$ on the axes below.

4. Below are three graphs.

Match each graph with one of the following equations.
Equation A: $\quad y=3 x-p$
Equation B: $\quad y=x^{2}+p$
Equation C: $\quad 3 x+4 y=p$
Equation D: $\quad y=p x^{3}$

In each case $p$ is a positive number.
(i)

(ii)

(iii)

Answer
Graph
(i) Equation
Graph
(ii) Equation $\qquad$
Graph (iii) Equation
5. Match each of the sketch graphs to one of these equations.
A $y=2-2 x$
B $y=2 x+2$
C $y=3-x^{2}$
D $y=x^{3}+4$
E $y=\frac{2}{x}$





Graph 1 represents equation $\qquad$
Graph 2 represents equation $\qquad$
Graph 3 represents equation $\qquad$
Graph 4 represents equation $\qquad$


Match each curve to its equation.
(a) $y=\frac{1}{x}$ is curve $\qquad$
(b) $y=2^{x}$ is curve $\qquad$
(c) $y=3^{x}$ is curve $\qquad$
(d) $y=\frac{4}{x}$ is curve $\qquad$

## Success:

## Target:

