| Nam | ie:  | Teacher<br>Assessment   |   | Topic 8 - F<br>Probability                   |
|-----|--|---|---|--|
| Sec | ction A  | Probabili   | ty Scale                                | Grade G $\rightarrow$ E                      |
| 1.  | A fair spinner has five sect<br>Two sections are red, one                |   | nd one is yellow.                       | Avenue book                                  |
|     | The spinner is spun once.  |   |   | Real White                                   |
|     | (a) Which colour is the  | spinner most likely to l  | and on?                                 |  |
|     |  |   | Answer                                  |  |
|     | (b) The probabilities of   | three events have been  | marked on the probabi                   | ility scale below.                           |
|     |  | A: The spinner lands<br>B: The spinner lands<br>C: The spinner does                 | on white.                               |  |
|     | L  | ↓ ↓   | ¥                                       |  |
|     | 0  |   |   | 1  |
|     | Label each arrow wi  | th a letter to show which   | ch event it represents.                 | (2)(Total A months)                          |
| 2.  | The probabilities of the fol   | lowing quanta have have   | on marked on the probe                  | (3)(Total 4 marks)                           |
| 2.  | <ul><li>A: The next baby born</li><li>B: The next vehicle to p</li></ul> | at the City Hospital will<br>pass the hospital will be<br>pass the hospital will he | l be a boy.<br>e a car.                 | ionity scale below.                          |
|     | ¥ .  |   | +                                       | _,   |
|     | 0  |   |   | 1  |
|     | Label each arrow with a le   | tter to show which even   | nt it represents.                       | (Total 2 marks)                              |
| 3.  | The boxes show some even<br>chance of the event happen                   |   | lowing words below ea                   | ach box to describe the                      |
|     | IMPOSSIBLE UI  | NLIKELY EV  | 'ENS LIKEL'                             | Y CERTAIN                                    |
|     | A person living to<br>the age of 100 years                               | dice lan  | ry six-sided<br>ding on a<br>ess than 7 | There will be eight<br>Sundays next<br>month |

.....

| St Paul's Catholic School |
|---------------------------|
|---------------------------|

.....

(Total 3 marks)

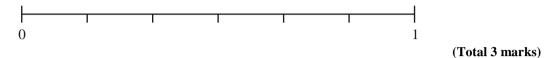
1

.....

4. A fair six-sided dice is thrown once.

Mark the probability of each of the following events onto the probability scale.

- A: The dice lands on the number 3.
- B: The dice lands on an odd number.
- C: The dice lands on a number greater than 2.

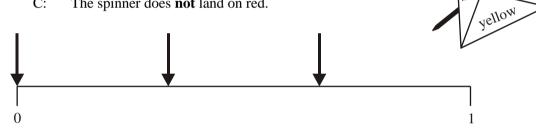


5. A fair spinner has three equal sections. One section is red, one is blue and one is yellow.

#### The spinner is spun once.

The probabilities of three events have been marked on the probability scale below.

- A: The spinner lands on blue.
- B: The spinner lands on green.
- C: The spinner does not land on red.



Label each arrow with the letter to show which event it represents.

6. A fair six-sided spinner is numbered from 1 to 6.

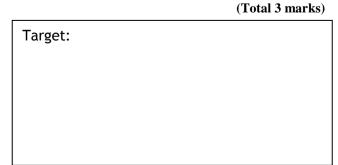
### The spinner is spun once.

Mark on the probability scale the probabilities of each of the following events.

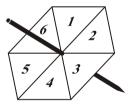
- А The spinner lands on an even number.
- В The spinner lands on a 4 or a 5.
- С The spinner lands on a number less than 7.







(Total 3 marks)



Teacher Assessment



Topic 8 - F Probability

## Section BCalculating ProbabilitiesGrade $F \rightarrow D$

**1.** This passage is from a reading book for Primary children.

Horatio was gazing into the night from his bedroom window. He was watching for aliens.

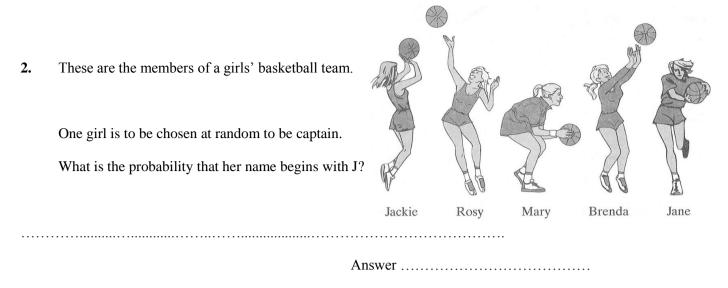
(a) Complete this frequency table by counting the number of letters in each word in the passage.

| Number of letters<br>in each word | Tally | Frequency |
|-----------------------------------|-------|-----------|
| 1                                 |       |           |
| 2                                 |       |           |
| 3                                 |       |           |
| 4                                 |       |           |
| 5                                 |       |           |
| 6                                 |       |           |
| 7                                 |       |           |
| 8                                 |       |           |
|                                   | Total |           |

(3)

(b) Write down the mode of the number of letters in a word.

|     | Answer   | (1)    |
|-----|--|--------|
| (c) | A word is chosen at random from the passage. Find the probability that the word has  |        |
|     | (i) exactly four letters,  |        |
|     | Answer   | (1)    |
|     | (ii) more than five letters.   |        |
|     | Answer   | (2)    |
| (d) | What do you think would happen to the average word length if a similar passage was chosen from an adult science fiction novel? |        |
|     |  |        |
|     | (1)(Total 8 n  | 1arks) |



#### (Total 2 marks)

**3.** Sami keeps her credit card receipts in a drawer until her statement arrives. The table shows the number of each type of receipt in the drawer.

| Petrol | Groceries | Hotels | Rail fares | Other |
|--------|-----------|--------|------------|-------|
| 5      | 8         | 1      | 2          | 4     |

Sami picks a receipt at random from the drawer. What is the probability that the receipt she picks is

(a) for hotels,

| Answer |     |
|--------|-----|
|        | (2) |

(b) **not** for hotels?

| Answer     |        |
|------------|--------|
|            | (1)    |
| (Total 3 I | narks) |

- **4.** (a) The list gives some words used in probability.
  - Impossible unlikely evens likely certain

For each of the events below, write down the word from the list which describes its probability.

(i) A fair coin landing on heads.

Answer .....(1)

(ii) Picking a red ball, at random, from a bag containing 20 red balls and 3 black balls.

Answer .....

- (iii) Throwing the number 8 on an ordinary fair six-sided dice.
  - Answer .....

(1)

(1)

(b) Brian has some red marbles, blue marbles and white marbles in a bag. He says that the probability of choosing each colour is shown in the table.

| Colour of marble | red | blue | white |
|------------------|-----|------|-------|
| Probability      | 0.3 | 0.6  | 0.2   |

There is a mistake in the probabilities in the table. Explain how you know this.

.....

(1) (Total 4 marks)

5. A fair ordinary six-sided dice is thrown once. The boxes show some of the possible outcomes.

Draw a line from each box in column A to the box in column B which has the same probability.

| Column A                     |   | Column B                     |                 |  |
|------------------------------|---|------------------------------|-----------------|--|
| Throwing<br>a six            |   | Throwing<br>an even number   |                 |  |
| Throwing<br>a two or a three |   | Throwing<br>a one            |                 |  |
| Throwing<br>an odd number    |   | Throwing<br>a four or a five | -               |  |
|                              | I   |                              | (Total 3 marks) |  |
| Susan and Jill play a game.  |   |                              |                 |  |
|                              | Susan has a box containing 3 red, 4 yellow and 2 blue counters. She picks a counter at random. What is the probability that Susan picks a yellow counter? |                              |                 |  |
|                              | Answei  | r                            |                 |  |

(b) Jill has a box containing 18 counters of which 8 are yellow. She picks a counter at random. What is the probability that Jill does **not** pick a yellow counter?

Answer .....

(c) Who is more likely to pick a yellow counter? Tick the correct box. Explain your answer.

| Susan       | Jill | Neither |                    |
|-------------|------|---------|--------------------|
| Explanation |      |         |                    |
|             |      |         |                    |
|             |      |         | (2)(Total 6 marks) |

6.

(2)

(2)

| 7. | (a)  | A box of chocolates contains 7 soft centres, 5 toffee centres and 8 nut centres.  | Topic 8 - F<br>Probability |
|----|------|---|----------------------------|
|    |      | Mary chooses a chocolate at random.   |                            |
|    |      | What is the probability that she chooses a chocolate with a toffee centre?  |                            |
|    |      |   |                            |
|    |      | Answer  | (2)                        |
|    | (b)  | In a bag of sweets the probability of choosing a sweet with a soft centre is 0.4 What is the probability of choosing a sweet that does <b>not</b> have a soft centre? |                            |
|    |      | Answer  | (1)                        |
|    |      |   | (Total 3 marks)            |
| 8. | A ba | g contains 12 blue and 8 green counters. A counter is chosen at random.   |                            |
|    | (a)  | Find the probability that the counter chosen is red.  |                            |
|    |      |   |                            |
|    |      | Answer  | (1)                        |
|    | (b)  | Find the probability that the counter chosen is green.<br>Give your answer as a fraction in its lowest terms.   |                            |
|    |      |   |                            |
|    |      | Answer  | (2)                        |
|    | (c)  | 10 yellow counters are added to the bag.  |                            |
|    |      | Calculate the probability that a counter chosen at random is green or yellow.   |                            |
|    |      |   |                            |
|    |      |   |                            |
|    |      |   |                            |
|    |      | Answer  |                            |
|    |      |   | (2)<br>(Total 5 marks)     |

| 9. | Mr K<br>Mrs l | raffle 200 tickets are sold. There is only one prize.<br>Ley buys 10 tickets.<br>Key buys 6 tickets.<br>r children, Robert and Rachel, buy 2 tickets each. | Trobability           |
|----|---------------|--|-----------------------|
|    | (a)           | Which member of the family has the best chance of winning the prize?<br>Give a reason for your answer.   |                       |
|    |               |  | (2)                   |
|    | (b)           | What is the probability that Mrs Key wins the prize?   | (2)                   |
|    |               | Answer   | . (2)                 |
|    | (c)           | What is the probability that <b>none</b> of the family wins the prize?   |                       |
|    |               |  |                       |
|    |               | Answer(7   | (3)<br>Fotal 7 marks) |

10. A bag contains blue, red and green cards only. One card is taken at random from the bag. The table shows the probabilities of taking a blue card and a red card.

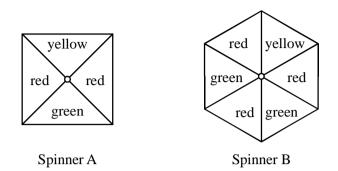
| Colour      | Blue | Red | Green |
|-------------|------|-----|-------|
| Probability | 0.3  | 0.5 |       |

(a) What is the probability of taking a yellow card from the bag?

|     | Answer  | (1)                    |
|-----|---|------------------------|
| (b) | What is the probability of taking a card that is <b>not</b> blue from the bag?  |                        |
|     | Answer  | <br>(1)                |
| (c) | Complete the table to show the probability of taking a green card from the bag. |                        |
|     |   | (1)<br>(Total 3 marks) |

#### **11.** Danny has two fair spinners.

Spinner A has four equal sections, two are red, one is yellow and one is green. Spinner B has six equal sections, three are red, one is yellow and two are green.

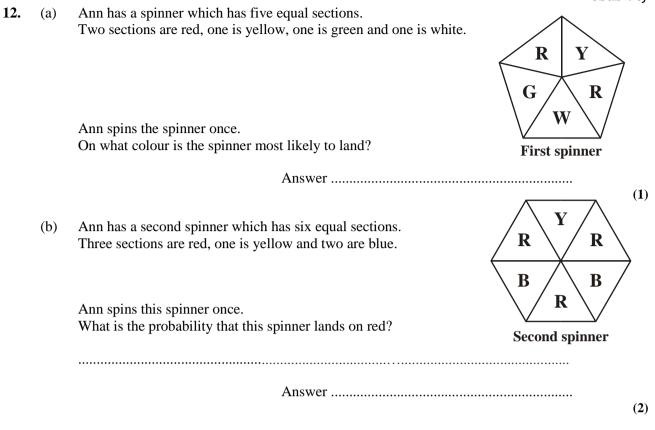


Danny spins each spinner once.

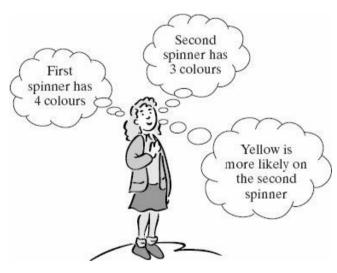
| (a) | Which colour is Spinner A most likely to land on?  |     |
|-----|--|-----|
|     | Answer   | (1) |
| (b) | Which spinner is more likely to land on yellow, Spinner A or Spinner B?  |     |
|     | Give a reason for your answer.   |     |
|     |  |     |
|     |  | (1) |
| (c) | What is the probability that Spinner A lands on green?   |     |
|     | Answer   | (1) |
| (d) | The probabilities of three events have been marked on the probability scale below.                                       |     |
|     | <ul> <li>R: Spinner B lands on red</li> <li>Y: Spinner B lands on yellow</li> <li>G: Spinner B lands on green</li> </ul> |     |
|     |  |     |

Label each arrow with a letter to show which event it represents.

(2) (Total 5 marks)



(c) Ann thinks that she has more chance of getting yellow on the second spinner.



Explain why Ann is wrong.

.....

.....

.....

(2) (Total 5 marks)

Success:

Target:

Teacher Assessment



Topic 8 - F Probability

### Section C

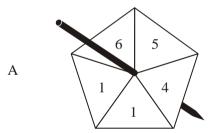
### **Listing Outcomes**

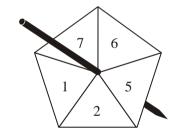
### Grade D

- 1. Lucy has two ordinary, fair dice. One dice is red and the other is blue. She rolls each dice once and adds the scores to get the total.
- Blue dice (a) Complete the table to show the totals. 1 2 3 5 4 6 (2) (b) What is the probability that Lucy gets a 1 total of 12? 2 Answer ..... (1) Red dice 3 4 (c) What is the probability that Lucy gets a total of 6? 5 Answer ..... 6 (2)(Total 5 marks)

В

2. Two fair spinners A and B are shown.



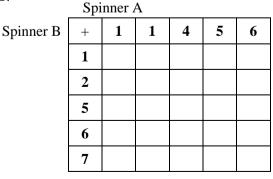


James plays a game using the two spinners. His score is the sum of the two numbers on spinner A and spinner B. He wins if his score is even.

.....

James plays the game many times.

Is he likely to win more times than he loses? You must show your working. You may use this table if you wish.



..... (Total 4 marks)

# **3.** Sarah is playing a game with a fair coin and a fair six-sided dice. She spins the coin and then throws the dice.

If the coin shows heads Sarah's score is 1 **more** than the number shown on the dice. If the coin shows tails Sarah's score is 2 **less** than the number shown on the dice.

(a) Complete the table to show all possible scores.

|         |             |             | Dice       |          |   |   |   |           |         |
|---------|-------------|-------------|------------|----------|---|---|---|-----------|---------|
|         |             | 1           | 2          | 3        | 4 | 5 | 6 |           |         |
| Coin    | Heads       |             |            |          | 5 |   |   |           |         |
|         | Tails       | -1          |            |          |   |   |   |           |         |
|         |             |             |            |          |   |   |   |           | (2      |
| Work ou | t the proba | ability tha | ıt Sarah's | score is |   |   |   |           |         |
| (i) ne  | gative      |             |            | Answer.  |   |   |   |           |         |
| (ii) mo | ore than 3. |             |            |          |   |   |   |           | (1      |
|         |             |             |            |          |   |   |   |           |         |
|         |             |             |            | Answer   |   |   |   | (2)(Total | 5 marks |

**4.** David is playing a game with a fair coin and a set of four cards. The cards are numbered 1, 2, 3 and 4. David spins the coin and then chooses a card at random.

If the coin shows heads David's score is the same as the number on the card. If the coin shows tails David's score is twice the number on the card.

(a) Complete the table to show all possible scores.

|     | Card   |         |         |        |   |   | 1 |         |             |
|-----|--|---------|---------|--------|---|---|---|---------|-------------|
|     |  |         |         | 1      | 2 | 3 | 4 |         |             |
|     |  | Coin    | Heads   |        | 2 |   |   |         |             |
|     |  |         | Tails   |        |   | 6 |   |         |             |
|     |  |         |         |        |   |   |   | -       | (2)         |
| (b) | (b) Work out the probability that David's score is |         |         |        |   |   |   |         |             |
|     | (i)  | 3       |         | Answer |   |   |   |         |             |
|     |  |         |         |        |   |   |   |         | (1)         |
|     | (ii)   | an even | number. |        |   |   |   |         |             |
|     |  |         |         |        |   |   |   |         |             |
|     |  |         |         | Answei |   |   |   |         |             |
|     |  |         |         |        |   |   |   | (2)(Tot | al 5 marks) |

(b)

5. Ashraf is playing a game with a fair coin and a fair triangular spinner with sections numbered 2, 3 and 4.



He flips the coin and then spins the spinner.

If the coin shows heads, his score is the number on the spinner **multiplied** by 3. If the coin shows tails, his score is the number on the spinner.

(a) Complete the table to show all the possible scores that Ashraf can get.

|      |       |   | Spinner |   |     |
|------|-------|---|---------|---|-----|
|      |       | 2 | 3       | 4 |     |
| Coin | Heads |   |         |   |     |
| Com  | Tails |   |         |   | (2) |
|      |       |   |         |   | ,   |

(b) Write down the probability that Ashraf gets a score of

| (i)  | 9,         | Answer |                        |
|------|------------|--------|------------------------|
| (ii) | 6 or less. | Answer | <br>(2)(Total 5 marks) |

6. Here is a pack of ten cards.



| Z |
|---|
| Γ |







Complete this two-way table to show the number of different cards in the pack.

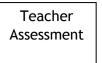
|           | Shaded | Unshaded | (2) |
|-----------|--------|----------|-----|
| Circles   |        |          |     |
| Triangles |        |          |     |

(b) One of the cards is picked at random.What is the probability that it has either a shaded circle or an unshaded triangle?

(a)

|          | ••••• |         | <br>                   |
|----------|-------|---------|------------------------|
|          |       |         | <br>                   |
| Answer   |       |         | <br>(2)(Total 4 marks) |
| Success: |       | Target: |                        |

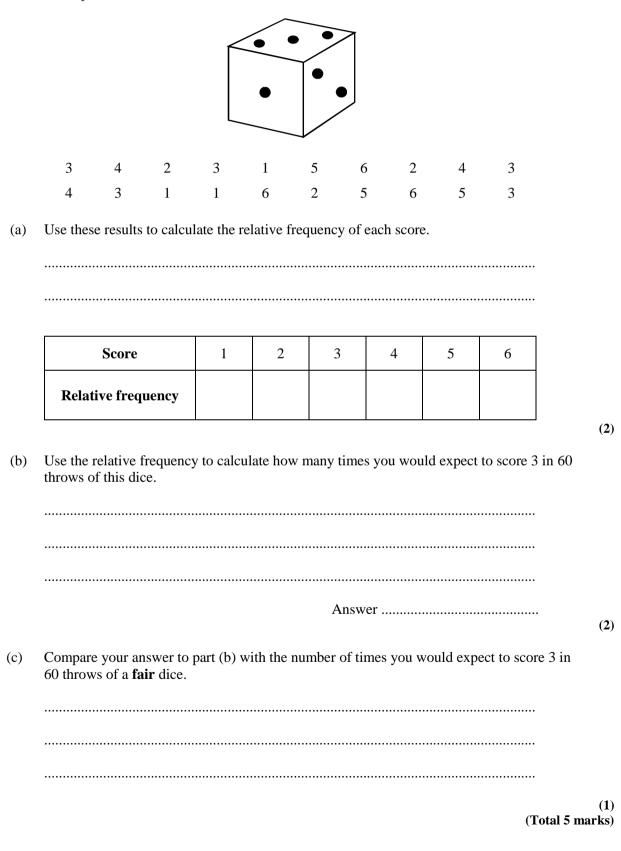
Spinner





### Section D Relative Frequency and Expectation Grade D / C

1. A dice is suspected of bias. Here are the results of 20 throws.



Answer .....

3.

|   | 1 1 |   |   |   |
|---|-----|---|---|---|
| В | Y   | Y | G | R |
| G | R   | Y | В | В |
| Y | R   | В | В | Y |
| В | В   | G | R | Y |

(a) Use these results to calculate the relative frequency of each colour.

.....

| Colour             | Red | Blue | Green | Yellow |
|--------------------|-----|------|-------|--------|
| Relative frequency |     |      |       |        |

(b) Use the results to calculate how many times you would expect a blue card if 100 pupils each choose a card at random.

|    | Answer   |               |                                       |  |  |  |
|----|--|---------------|---------------------------------------|--|--|--|
|    |  |               | (2)(Total 4 marks)                    |  |  |  |
|    | blue, white and green tickets are sold in a raff<br>table shows some of the probabilities of these t               |               | 2.                                    |  |  |  |
| a) | Calculate the probability of a green   | Ticket colour | Probability of winning<br>first prize |  |  |  |
|    | ticket winning the first prize.  | Red           | 0.4                                   |  |  |  |
|    |  | Blue          | 0.2                                   |  |  |  |
|    |  | White         | 0.1                                   |  |  |  |
|    |  | Green         |                                       |  |  |  |
|    | Answer   |               | (2)                                   |  |  |  |
| b) | There were 1000 tickets sold in this raffle. Calculate how many red tickets and blue tickets were sold altogether. |               |                                       |  |  |  |

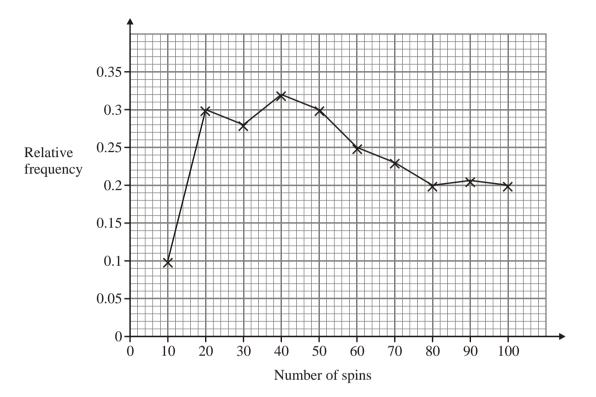
.....

(2)(Total 4 marks)

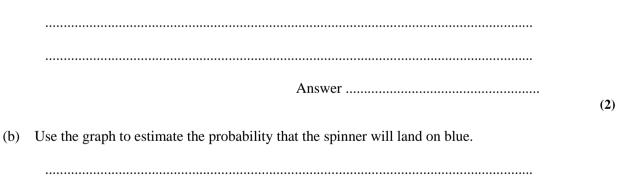
(2)

Topic 8 - F Probability

 Lynne has a spinner with coloured sections of equal size. She wants to know the probability that her spinner lands on blue. She spins it 100 times and calculates the relative frequency of blue after every 10 spins Her results are shown on the graph.



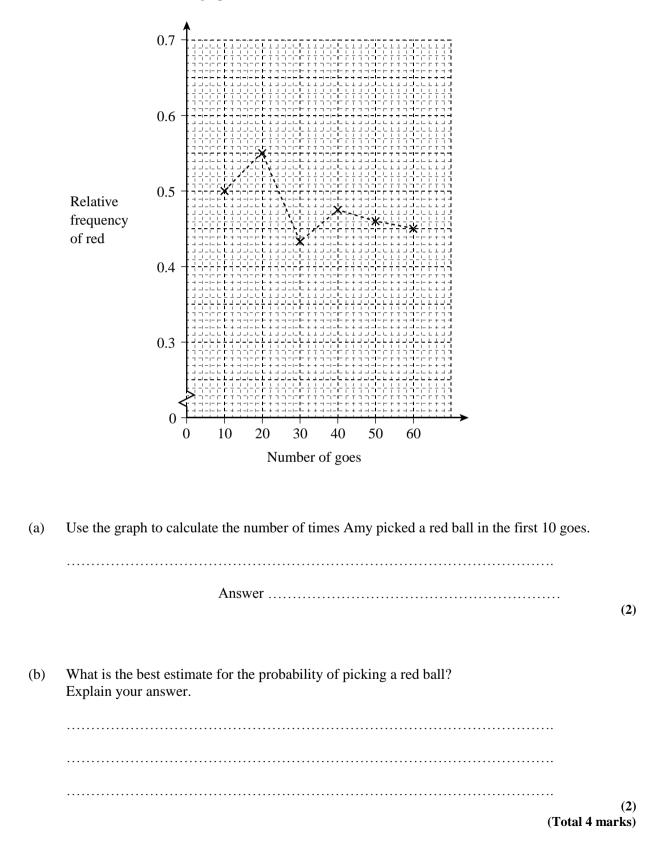
(a) Use the graph to calculate the number of times the spinner landed on blue in the first 20 spins



Answer .....

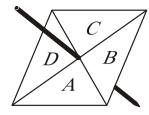
(1) (Total 3 marks) 5. Amy has a bag containing red, green and blue balls.

She wants to know the probability of picking a red ball from the bag. She picks a ball at random from the bag, records the colour and replaces the ball in the bag. Amy does this 60 times and calculates the relative frequency of red after every 10 goes. Her results are shown on the graph.



Topic 8 - F Probability

6. A four-sided spinner has sections labelled A,B,C,D.

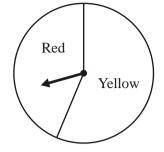


The spinner is spun and the relative frequency of the letter A is recorded after every 10 spins.

| 1 101 1118   |                                  | ere 20 letters As.<br>ency on the diag  |               | 0.6 |               |           |               |               |
|--|----------------------------------|---|---------------|-----|---------------|-----------|---------------|---------------|
|  | ·····                            |   |               | 0.5 | _ <del></del> |           |               |               |
|  |                                  |   |               |     |               |           |               |               |
|  |                                  | (1)                                     | Relative      | 0.4 |               |           | - <b>x</b>    | *             |
|  |                                  |   | frequency     | 0.3 |               | *         |               |               |
|  |                                  |   |               | 0.2 |               |           |               |               |
|  |                                  |   |               | 0.1 |               |           |               |               |
|  |                                  |   |               | 0   |               |           |               |               |
|  |                                  | the first 60 spins<br>inner land on A i |               | Ó   | 10            | 20<br>Nun | 30<br>nber of | 40 5<br>spins |
|  |                                  | Answer                                  |               |     |               |           | ••••          | (1            |
| is the spinner b   | iased? Give a                    | reason for your                         | answer.       |     |               |           |               |               |
| -  |                                  |   |               |     |               |           |               |               |
|  |                                  |   |               |     |               |           |               |               |
|  |                                  |   |               |     |               |           |               | (2            |
|  | 1000 1                           |   |               |     |               |           |               |               |
| The spinner is s<br>How many time                          |                                  | expect the spinn                        | er to land on | A?  |               |           |               |               |
|  |                                  | expect the spinn                        |               |     |               |           |               |               |
|  |                                  |   |               |     |               |           |               | (2            |
| How many time  | es would you                     | expect the spinn                        |               |     |               |           |               | (2            |
| How many time  | es would you                     | Answer                                  |               |     |               |           |               | (2            |
| How many time  | es would you                     | Answer<br>C D                           |               |     |               |           |               | (2            |
| How many time<br>A different four<br>Letter<br>Probability | r-sided spinne<br>A B<br>0.2 0.3 | Answer<br>C D                           | abilities.    |     |               |           |               | (2            |
| How many time<br>A different four<br>Letter<br>Probability | r-sided spinne<br>A B<br>0.2 0.3 | Answer<br>er has these proba            | abilities.    |     |               |           |               | (2            |

| (a)   | What is the probability that Alan or Bob wins the game?   |           |
|-------|---|-----------|
| . ,   |   |           |
|       |   |           |
|       | Answer  |           |
| (b)   | Alan, Bob and Colin play 20 games of darts. How many games would you expect C win?                        | olin to   |
|       |   |           |
|       |   |           |
|       |   |           |
|       |   |           |
|       | Answer  |           |
|       | Γ)  | Total 5 n |
| The o | g contains 200 coloured discs.<br>discs are either red, blue or yellow.<br>e are 86 red discs in the bag. |           |
|       | probability that a blue disc is chosen from the bag is 0.22   |           |
|       | ulate the number of yellow discs in the bag.  |           |
| Calcu |   |           |
|       |   |           |
|       |   |           |
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9. A spinner has a red sector (R) and a yellow sector (Y).



The arrow is spun 1000 times.

The table shows the relative frequency of a red after different numbers of spins.

| Number of spins | Relative frequency<br>of a red |
|-----------------|--------------------------------|
| 50              | 0.42                           |
| 100             | 0.36                           |
| 200             | 0.34                           |
| 500             | 0.3                            |
| 1000            | 0.32                           |

(a) How many times was a red obtained after 200 spins?

| Answer | (2) |
|--------|-----|

(b) Which relative frequency gives the best estimate of the probability of a red? Explain your answer.

.....

(2) (Total 4 marks)

#### 10. Penny, Sam and Robert do this experiment on the same bag of 10 counters.

- 1. Take a counter from the bag at random.
- 2. Record its colour.
- 3. Put the counter back in the bag.

Repeat this trial a number of times.

Their results are shown in this table.

| Name of | Number    | Colour of counter |       |       |  |  |  |
|---------|-----------|-------------------|-------|-------|--|--|--|
| pupil   | of trials | Black             | White | Green |  |  |  |
| Penny   | Penny 10  |                   | 6     | 4     |  |  |  |
| Sam     | 40        | 3                 | 16    | 21    |  |  |  |
| Robert  | 200       | 22                | 76    | 102   |  |  |  |

Estimate the number of each different coloured counter in the bag. Clearly state the set of results that you use to make the estimate. Give a reason for your choice.

|         |                    |      |         | ••              |
|---------|--------------------|------|---------|-----------------|
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|         |                    |      |         |                 |
|         |                    |      |         |                 |
|         |                    |      |         |                 |
|         | et of results used |      |         |                 |
|         | Answer Black, Wh   | nite | , Green |                 |
|         |                    |      |         | (Total 4 marks) |
| Success | :                  |      | Target: |                 |
|         |                    |      |         |                 |