

2 Formulae

2.4 Substitution into Formulae

1. The speed of a bike, v metres per second, is given by the formula

$$v = u + ft$$

when u is its initial speed (in m/s), f its acceleration (in m/s²) and t , the time in seconds.

Determine v when

- (a) $u = 0$, $f = 5$ and $t = 10$ (b) $u = 20$, $f = 2$ and $t = 5$
(c) $u = 20$, $f = 0$ and $t = 5$ (d) $u = 40$, $f = -5$ and $t = 5$
(e) $u = 40$, $f = -5$ and $t = 8$

In each case, briefly describe the motion of the bike.

2. The Fahrenheit scale, (F) and the Celsius scale (C) are related by the formula

$$F = \frac{9}{5}C + 32$$

- (a) Give the following temperatures in Fahrenheit.
(i) Normal body temperature: 37 °C
(ii) Boiling point of water: 100 °C
(b) Give the following temperatures in degrees Celsius.
(i) Freezing point of water: 32 °F
(ii) Singapore's average daily temperature: 86 °F
3. If $x = 3$, $y = 4$ and $z = 7$, find the values of the following expressions:

- (a) $5yz$ (b) xyz (c) $\frac{12}{xy}$
(d) $\frac{xy}{18}$ (e) $2x + 3y$ (f) $x - 5y + 2z$
(g) $xy + yz$ (h) $x^2 + y^2$ (i) $2z^2 + y$
(j) $y^2 + x^3$ (k) xy^2 (l) $4x^2y^2$

4. If $a = 3$, $b = 2$ and $c = -1$, find the value of each of the following.

- (a) $a^3 + b^3 + c^3 - 2abc$ (b) $(2a + b - c)(4b - 3c)$
(c) $(a - b)^2 - (b - c)^2$ (d) $\frac{a}{b} + \frac{b}{c} - \frac{c}{a}$
(e) $\frac{a+1}{2} - \frac{b+c}{4} + \frac{c-a}{3}$ (f) $a^b - c^a + b^a$

(g) $2a - 3b^2 + 3abc^2$	(h) $a^2 + 3b^3 - 4c^5$
(i) $\frac{a+b}{c} - \frac{ab-c}{b}$	(j) $\frac{3a-b}{b-c} + \frac{a+c}{b-a}$
(k) $\frac{2c^2-3a}{bc-a} - \frac{4b}{3a}$	(l) $\frac{a^2-b^2}{c^2} - \frac{a^3-c}{(c-3b)}$

5. Find the value of $x^3 + 2xy^2 + y^3$ when $x = 2$ and $y = -1$.

6. Find the value of $\frac{x+1}{x-1} + \frac{2x-1}{2x+1}$ when $x = -2$.

7. Find the value of $2ab + 3bc^2$ when $a = 0$, $b = 5$ and $c = -2$.

8. The distance travelled, s metres, by a car is given by

$$s = ut + \frac{1}{2}ft^2$$

Here u is the car's initial speed (in m/s), t the time (in seconds) and f the acceleration (in m/s²).

(a) Find s when

(i) $u = 0$, $t = 10$, $f = 5$

(ii) $u = 20$, $t = 5$, $f = 6$

(iii) $u = 50$, $t = 4$, $f = -5$

(iv) $u = 60$, $t = 10$, $f = -2$

(b) If the car travels 400 metres in 5 seconds with initial speed of 40 m/s, what is its acceleration?

2.5 More Complex Formulae

1. It is given that $v^2 = u^2 + 2as$. Find the values of u when $v = 0.8$, $a = 0.05$ and $s = 2.8$.

2. It is given that $y = \frac{18-5x}{2y}$. Find

(a) the values of y if $x = -6.4$

(b) x if $y = 2\frac{1}{2}$

3. If $S = \frac{n}{2}[2a + (n-1)d]$, find

(a) the value of S when $n = 10$, $a = -2$ and $d = \frac{1}{2}$

(b) a when $S = 440$, $n = 10$ and $d = 5$.

4. The arithmetic mean, A , geometric mean, G , and harmonic mean, H , of three numbers, are given by the formulae

$$A = \frac{a + b + c}{3}, \quad G = (abc)^{\frac{1}{3}}, \quad H = \frac{3}{\left(\frac{1}{a} + \frac{1}{b} + \frac{1}{c}\right)}$$

Find A , G and H for the following sets of numbers.

- (a) $a = 2, b = 3, c = 4$ (b) $a = 1, b = 3, c = 5$
 (c) $a = b = c = 3$ (d) $a = 2.5, b = 3, c = 3.5$

What do you notice about the values of A , G and H ?

5. Find z , given by each of the following formulae, for the given values of x and y .

(a) $\frac{1}{z} = \sqrt{\frac{1}{x^2} + \frac{1}{y^2}}, \quad x = 2, \quad y = 3$

(b) $z^2 = x^2 + y^2, \quad x = 3, \quad y = -4$

(c) $\frac{1}{z} = \frac{x + y}{x^2 + y^2}, \quad x = -2, \quad y = 4$

(d) $\frac{x}{z} = \frac{x}{y} + 1, \quad x = 5, \quad y = 2$

(e) $\frac{1}{z^2} = \frac{1}{x^2} + \frac{1}{y^2}, \quad x = 4, \quad y = 3$

6. The formula $v^2 = u^2 + 2fs$ connects the initial, (u), and final, (v), speeds of a car, with its acceleration, (f), and distance travelled, (s).

Find v (in m/s) when

- (a) $u = 0, f = 10 \text{ m/s}^2, s = 100 \text{ m}$
 (b) $u = 20 \text{ m/s}, f = 5 \text{ m/s}^2, s = 50 \text{ m}$
 (c) $u = 75 \text{ m/s}, f = -10 \text{ m/s}^2, s = 25 \text{ m}$

2.6 Changing the Subject

1. Make s the subject of each of the following:

(a) $2s - 8p = 14$ (b) $28 = 4s + r - s$ (c) $10 - 2s = 12r + 2s$

2. In each of the following, make y the subject:

(a) $y + x = 6$ (b) $m + y = 2 - n$ (c) $\frac{k}{5} = \frac{y}{3}$

(d) $3 + m = d + y$ (e) $5 = y - 3m$ (f) $2y + 6 = 48 + 2x$

3. (a) Given that $4a + b = c - a$, express a in terms of b and c .
 (b) Given that $x - y = 3z$, express y in terms of x and z .
 (c) Given that $pq = r$, express q in terms of p and r .
 (d) Given that $a + b = 8c + 7$, express c in terms of a and b .

4. Make a the subject of the following formulae:

- (a) $a + x = b$ (b) $a + h = k$ (c) $a - m = n$
 (d) $a - k = h$ (e) $a - b = c + d$ (f) $a + c = d + e$
 (g) $y + a = x$ (h) $z - a = 2k$ (i) $p = a - q$
 (j) $5k = p - a$ (k) $7k = p + a$ (l) $a - b - c = k^2$
 (m) $b - a + k = h^3$ (n) $m + n + a = k$ (o) $m - n - a = h$
 (p) $7k - h - a = 2a$ (q) $5pq - a = p^2 - q$ (r) $3xy + a = x^2y$
 (s) $5a = 15$ (t) $ax = 3y$ (u) $xay = 3k$
 (v) $2xy = 3ak$ (w) $ak = p - q + k$ (x) $ax^2 = 5y - 4$

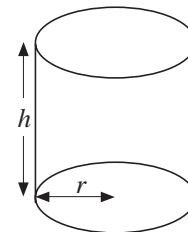
5. Make a the subject of the given formula.

- (a) $ax = y$ (b) $a(p - 4) = q$ (c) $ax + by = c$
 (d) $p(a + b) = c$ (e) $2a - 3m = 4a - 7$ (f) $5b - 2a = 3c$
 (g) $\frac{a}{m} + b = c$ (h) $x = \frac{2a}{3} + 5z$ (i) $\frac{p + a}{5} = 3p$
 (j) $R = m(a + g)$ (k) $2b = ax + a$ (l) $2m = 65 - 4a$

6. (a) The volume of a cylinder is given by

$$V = \pi r^2 h$$

- (i) Make h the subject of this equation.
 (ii) Find h when $r = 3$ cm and $V = 350$ cm³.

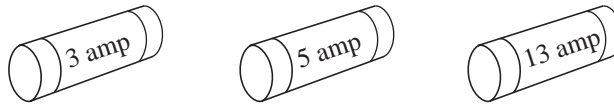


(b) The total surface area is given by

$$s = 2\pi r^2 + 2\pi rh$$

- (i) Make h the subject of this equation.
 (ii) Find h when $r = 3$ cm and $s = 300$ cm².

7. Electrical fuses are available as shown.



The correct fuse to use for an electrical appliance can be calculated using this formula,

$$F = \frac{P}{240}$$

where

F = Fuse rating in amps,

P = Power rating in watts.

- (a) Which fuse should be fitted for a toaster with power rating 1100 watts?
- (b) An electric heater needs a 13 amp fuse. What is the largest power rating the heater could have?
- (SEG)
8. The length of a man's forearm (f cm) and his height (h cm) are approximately related by the formula

$$h = 3f + 90$$

- (a) Part of the skeleton of a man is found and the forearm is 20 cm long. Use the formula to estimate the man's height.
- (b) A man's height is 162 cm. Use the formula to estimate the length of his forearm.
- (c) George is 1 year old and he is 70 cm tall. Find the value the formula gives for the length of his forearm and state why this value is impossible.
- (d) Use the formula to find an expression for f in terms of h .
- (MEG)

2.7 Further Change of Subject

1. The volume of a cylinder is given by

$$V = \pi r^2 h$$

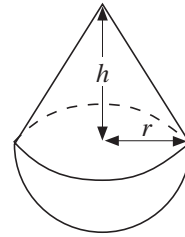
where r is the base radius and h the height.

- (a) Make r the subject of the formula.
- (b) Find r when $V = 300 \text{ cm}^3$ and $h = 5 \text{ cm}$

2. The volume of a toy, consisting of a base hemisphere and cone top, is given by

$$V = \frac{1}{3}\pi r^2 h + \frac{2}{3}\pi r^3$$

Make h the subject of this equation and find h when $V = 300 \text{ cm}^3$ and $r = 3 \text{ cm}$.



3. The surface area of a sphere is given by

$$S = 4\pi r^2$$

- (a) Make r the subject of this equation.
 (b) Find r when (i) $S = 100 \text{ cm}^2$ (ii) $S = 200 \text{ cm}^2$
 By what factor does the radius change when the surface area is doubled?

4. Make x the subject of

- (a) $y = 4x + 2$ (b) $y = 1 - 3x$ (c) $y = mx + c$
 (d) $y = \frac{1}{x+1}$ (e) $y = 1 + \sqrt{x}$ (f) $y = \frac{1}{1 + \sqrt{x}}$
 (g) $y = \sqrt{\frac{5x}{a}}$ (h) $y = \sqrt{x+1}$ (i) $\frac{1}{y} = \frac{1}{x} + 1$
 (j) $\frac{1}{y} = \frac{2}{3} - \frac{1}{x}$ (k) $y = \frac{1}{4} + \frac{1}{x}$ (l) $y = \frac{4}{\sqrt{2+x}}$

5. If $\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$, make u the subject of this formula. Find u when

- (a) $f = 5$ and $v = 1$ (b) $f = 3$ and $v = -2$

6. The percentage profit, p , on the sale of an item is given by the formula

$$p = \frac{100(s - c)}{c}$$

where s is the selling price and c is the cost price.
 Express c in terms of s and p .

(MEG)

7. Students conduct an experiment to find g , the acceleration due to gravity.

They measure the time, T seconds, for one complete swing of a pendulum of length L centimetres.

The formula for g is

$$g = \frac{4\pi^2 L}{T^2}$$

- (a) Find g when $L = 39.24$ and $T = 1.26$.
 Take $\pi = 3.142$ or use the π button on your calculator.
 (b) Rearrange the formula to express T in terms of L , π and g .

(SEG)

2.8 Expansion of Brackets

1. Copy and complete the following multiplication tables. Some have been done for you.

(a)

x	$y - 2$	$3y$	$\frac{6}{y}$	$4 - 3y$
-1		$-3y$		
$\frac{1}{4}$				$1 - \frac{3}{4}y$
2				
$-\frac{1}{2}$			$-\frac{3}{y}$	

(b)

x	$-k$	$\frac{2k}{3}$	$\frac{2}{3k}$	$2 - 2k$
6	$-6k$			
-4			$-\frac{8}{3k}$	
3				
$-\frac{1}{2}$				

2. Remove the brackets in each of the following algebraic expressions.

(a) $2(u - 3)$

(b) $8(v + 7)$

(c) $4(2x + 3y)$

(d) $6(5a - b)$

(e) $-2(p - q)$

(f) $-5(a + b)$

(g) $-3(-2u - 3v)$

(h) $8(-2u - 3v)$

(i) $\frac{1}{2}(10p - 6q)$

(j) $\frac{1}{5}(20x - 15)$

(k) $-(b + c)$

(l) $-(p - q)$

(m) $-x(p + q)$

(n) $-y(-x + y)$

(o) $-(-p - q)$

(p) $-(-t + r)$

(q) $\frac{1}{2}\left(\frac{2}{3}a - \frac{4}{5}b\right)$

(r) $6a\left(\frac{1}{3}b - \frac{5}{6}c\right)$

3. Simplify each of the following algebraic expressions.

(a) $(3x - 2y) + (4x - y)$

(b) $(p - m) + (m - 2p)$

(c) $5(x - 2) + 3(4 - x)$

(d) $(3a + 2b) - (a - b)$

(e) $2(3m + n) - 3(m - 3n)$

(f) $(x - y) - (y - z) - (z - x)$

(g) $3a(b - c) + (3b - 2)a$

(h) $m(m - n) - n(n - m)$

(i) $x(y - z) + y(z - x) + z(x - y)$

(j) $3(2y + 5z) - 4(2y - x)$

4. Multiply out and simplify each of the following expressions.

(a) $6(3x + y)$

(b) $5z(z - 2y)$

(c) $\frac{1}{2}(2xy - 4yz)$

(d) $q(p + 2r - 3s)$

(e) $(p + q)(r + s)$

(f) $(x + y)(z + 2w)$

(g) $(3a + b)(a + c)$

(h) $(m + 2n)(2p + 3q)$

(i) $(a - b)(c + d)$

(j) $(2e - f)(2g - h)$

(k) $(3p - 4q)(s + 2t)$

(l) $(a + 7)(2b + 5)$

(m) $(x + 3)(x + 4)$

(n) $(a + 5)(a - 3)$

(o) $(x - 7)(x - 6)$

(p) $(3 + c)(6 - c)$

(q) $(1 - 3x)(4 + 3x)$

(r) $(2p + 3)(p + 5)$

(s) $(4x + 5y)(2x + 3y)$

(t) $(d - 7)(d - 5)$

(u) $(a + 5)^2$

(v) $(x - 3)^2$

(w) $(b + 2)^2$

(x) $(e - 4)^2$

(y) $(2x + 1)^2$

(z) $(3x - 2)^2$

2.9 Factorisation

1. Factorise the following:

(a) $2x + 4$

(b) $9 - 3x$

(c) $2 + 10x$

(d) $-5 - 15x$

(e) $x^2 + 2x$

(f) $x - 3x^2$

(g) $4x + 2x^2$

(h) $3x^2 - 9x$

(i) $10x - 5x^2$

(j) $7x^2 + 21$

(k) $3x^2 - x^3$

(l) $2x + 8x^3$

(m) $2x^3 + 10x^2$

(n) $4x^2 - 4$

2. The following expressions have been partly factorised.

Complete the factorisation.

(a) $2x^2 - 4x = 2(x^2 - 2x) = ?$

(b) $10x - 5x^2 = x(10 - 5x) = ?$

(c) $4x^3 + 8x = 4(x^3 + 2x) = ?$

(d) $8xy + 16x^2 = x(8y + 16x) = ?$

(e) $5xy + 10x^2y^2 = 5(xy + 2x^2y^2) = ?$

3. Factorise the following:

(a) $10a - 15b$

(b) $50py - 120p$

(c) $24abc - 8ab$

(d) $6abc + 12bcd$

(e) $16m^2 + 12n^2$

(f) $p^2y + p^2y^2$

(g) $18s^2t - 12st^2$

(h) $10a + 15a^2$

(i) $c - c^2$

(j) $2a^2b^2 - 8a^2b$

(k) $m^2n - mnl$

(l) $6xy - 3y + 9x$

(m) $pqr + p^2 + pr$

(n) $abc + a^2b + bc$

(o) $8abc + 6ab^2c + 4abc^2$

(p) $5s^2t - 3st - 4st^2$

2.10 Algebraic Manipulation

1. Make a the subject of each of the following formulae.

(a) $\frac{k(m+a)}{m} = \frac{4}{x}$

(b) $5(a-b) = 7$

(c) $v = m(a+c)$

(d) $y = \frac{7ab+k}{7-4a}$

(e) $z = \frac{5-2a}{3-a}$

(f) $x = \frac{7+3a}{a-4}$

(g) $y = \frac{x^2a-b}{a-4}$

(h) $z = \frac{4ab+5c+2}{2ax+5y}$

2. Make the letters in brackets the subject of the following formulae.

(a) $(x+p)a = q(2x-q)$ (x) (b) $\frac{an-5x}{3a-4x} = \frac{1}{3}$ (a)

(c) $a = \frac{2b+c}{b}$ (b) (d) $\frac{y-2x}{3y} = 2x-7$ (x)

(e) $T = \frac{4pr}{p+4s}$ (p) (f) $\frac{1}{v} + \frac{2}{u} = \frac{3}{f}$ (u)

(g) $x = \frac{y}{2-y}$ (y) (h) $x = \frac{x+y-2}{x-y+1}$ (y)

(i) $w = \frac{a-b}{ac-1}$ (a) (j) $y = \frac{ax+b}{cx+d}$ (x)

(k) $\frac{1}{v} = \frac{u}{f} - 1$ (f) (l) $xy - 1 = 5(2x+3)$ (x)

(m) $\frac{F+40}{9} = \frac{c+40}{5}$ (c) (n) $P = \frac{ER}{k+R}$ (k)

(o)	$k = \frac{2x-1}{x+4}$	(x)	(p)	$3h = k\left(\frac{x}{2} - y\right)$	(x)
(q)	$P - mg = \frac{mv^2}{r}$	(m)	(r)	$c = \frac{nE}{k+na}$	(n)
(s)	$\frac{3}{5} = \frac{y-4a}{y+7b}$	(y)	(t)	$\frac{a}{k} + h = \frac{b}{k}$	(k)
(u)	$\frac{1}{a} + \frac{2}{b} = \frac{3}{c} + \frac{4}{d}$	(b)			

3. Make a the subject of the following formulae.

(a)	$\sqrt{a} = b$	(b)	$\sqrt{2a} = b$	(c)	$\sqrt{m+a} = b$
(d)	$e = \sqrt{5a-8}$	(e)	$\sqrt{\frac{a}{2}} = b$	(f)	$l = \sqrt{\frac{k}{ma}}$
(g)	$x = \sqrt{\frac{2a}{5c}}$	(h)	$\sqrt{3a-2} = \sqrt{\frac{a}{b}}$	(i)	$\sqrt{3a-2k} = z$
(j)	$2a^2 = b-3$	(k)	$3a^2 - 2 = 3c$	(l)	$k = ba^2 + z$
(m)	$b = \sqrt{\frac{a^2}{5c}}$	(n)	$m = n + \frac{na^2}{b}$	(o)	$A = 4\pi a^2$
(p)	$\sqrt[3]{a-b} = c$				

4. Make the letter in brackets the subject of the formula.

(a)	$a = \sqrt{a+2b}$	(b)	$a^2 + b^2 = c^2$	(b)
(c)	$(x+y)^2 = x$	(y)	$e = \sqrt{3c-7a}$	(c)
(e)	$x = 2w^2 + b$	(w)	$\sqrt[3]{y-1} = z$	(y)
(g)	$\frac{a^2}{x^2} + \frac{b^2}{y^2} = 1$	(b)	$\sqrt[3]{2x^2-7} = \frac{y}{z}$	(x)
(i)	$t = \sqrt{\frac{4x^2}{m-3}}$	(x)	$t^2 = \sqrt{\frac{m+2}{m-5}}$	(m)
(k)	$\frac{1}{a} - \frac{1}{b} = \frac{1}{c-2}$	(c)	$y = \frac{nx}{a(4x-3)}$	(x)

5. Find the value of x by making x the subject of each of the following.

(a)	$\frac{2}{5x} = \frac{4}{(x-1)}$	(b)	$\frac{5}{x} + \frac{1}{4} = \frac{3}{7}$
(c)	$\frac{2x}{2x+3} = 2$	(d)	$\frac{x+2}{3} = \frac{2x-1}{14}$

(e)
$$\frac{3}{(x+1)} + \frac{1}{(2x+1)} = 0$$

(f)
$$\frac{3x}{8} - \frac{x}{4} = \frac{1}{2}$$

2.11 Algebraic Fractions

1. Simplify each expression into a single fraction.

(a)
$$\frac{x}{4} + \frac{x}{8}$$

(b)
$$\frac{x}{6} - \frac{x}{12}$$

(c)
$$\frac{x}{5} + \frac{x}{10}$$

(d)
$$\frac{2x}{3} - \frac{x}{6}$$

(e)
$$\frac{x}{2} - \frac{x}{8}$$

(f)
$$\frac{4x}{7} - \frac{x}{9}$$

(g)
$$\frac{5}{a} + \frac{10}{b}$$

(h)
$$\frac{1}{2a} - \frac{1}{3b}$$

(i)
$$\frac{3}{a} + \frac{2}{3b}$$

2. Express the following as fractions with a single denominator.

(a)
$$\frac{x}{2} + \frac{x-1}{4}$$

(b)
$$\frac{3y}{4} - \frac{y-1}{2}$$

(c)
$$\frac{z}{2} - \frac{x+2}{3}$$

(d)
$$\frac{1}{3x} - \frac{1}{3y}$$

(e)
$$\frac{4}{ac} + \frac{2}{ab}$$

(f)
$$3 - \frac{n-p}{m}$$

(g)
$$\frac{4x^3y^2}{8xy^2} - \frac{x^2}{4}$$

(h)
$$a + \frac{b}{ca} - \frac{c}{ab}$$

(i)
$$\frac{3ab}{5x} - \frac{ab}{2x} - \frac{ab}{10x}$$

(j)
$$\frac{2y+1}{5} - \frac{3y-2}{10} + \frac{y}{2}$$

(k)
$$\frac{b+4}{6} - \frac{b}{3} + \frac{b-3}{12}$$

(l)
$$\frac{a}{2} + \frac{a}{3} - \frac{3a}{8}$$

(m)
$$\frac{c-1}{5} - \frac{2c+3}{3}$$

(n)
$$\frac{2y-3}{3} + \frac{y-2}{4}$$

(o)
$$\frac{a+1}{5} - \frac{a+1}{10} - \frac{a}{15}$$

(p)
$$\frac{e-4}{5} + 1$$

(q)
$$\frac{2}{3}(x-y) - \frac{3}{5}(x+y)$$

(r)
$$\frac{1}{3x} + \frac{1}{5x}$$

3. Simplify the following algebraic fractions.

(a)
$$\frac{x}{2} + \frac{x-3}{3} - \frac{x-4}{4}$$

(b)
$$\frac{2x-y}{2} + \frac{x-y}{3}$$

(c)
$$\frac{x+y}{2} - \frac{x+5y}{4} + \frac{5x-4y}{8}$$

(d)
$$\frac{2x-3y}{5} - \frac{x-6y}{10} + \frac{5x+6y}{15}$$

4. Express the following as fractions with a single denominator.

$$(a) \frac{1+x}{3} + \frac{x-5}{6}$$

$$(b) \frac{1}{3x} - \frac{2}{5y}$$

$$(c) \frac{x+1}{2} - \frac{x-3}{3}$$

$$(d) \frac{2(x+y)}{x} + \frac{3(x-3y)}{5x}$$

$$(e) \frac{5}{x-y} - \frac{7}{y-x}$$

$$(f) \frac{1}{a} - \frac{2}{a+b}$$

$$(g) \frac{x}{a-b} - \frac{1}{b-a}$$

$$(h) 3 - \frac{x-2}{3x}$$

5. Simplify:

$$(a) \frac{c}{3} - \frac{c}{6}$$

$$(b) \frac{x}{10} + \frac{2x}{5}$$

$$(c) \frac{y}{2} + \frac{3}{4}$$

$$(d) \frac{2x}{3} + \frac{x-1}{5}$$

$$(e) \frac{2x+3}{4} - \frac{3x-2}{12}$$

$$(f) \frac{u-2}{3} + \frac{2u+3}{9}$$

$$(g) v + \frac{1}{v}$$

$$(h) 2y + \frac{1}{y}$$

$$(i) m - \frac{2}{3m}$$

$$(j) \frac{1}{6x} + \frac{1}{3x}$$

$$(k) \frac{1}{2x} + \frac{3}{4x}$$

$$(l) \frac{3}{4y} - \frac{2}{y}$$

$$(m) \frac{1}{2} - \frac{1}{x-2}$$

$$(n) \frac{1}{m} + \frac{5}{mn}$$

$$(o) \frac{1}{p+q} + \frac{2}{3p+3q}$$

$$(p) \frac{8}{x+y} - \frac{3}{4x+4y}$$

$$(q) \frac{7}{x-y} + \frac{2}{5x-5y}$$

$$(r) \frac{5}{r-t} + \frac{1}{3r-3t}$$

$$(s) \frac{3}{x+1} - \frac{2}{x-1}$$

$$(t) \frac{5}{x-2} + \frac{7}{x+3}$$

$$(u) \frac{1}{x+2} + \frac{4}{x-1}$$

$$(v) \frac{2}{x-2} + \frac{6}{x-3}$$

$$(w) \frac{x}{4} + \frac{3(x-2)}{5}$$

$$(x) \frac{2y+3}{3} - \frac{2(y-1)}{7}$$